

Definition of the Derivative Practice

Interpret each of the following as a derivative. Evaluate if possible.

$$1. \lim_{x \rightarrow \frac{\pi}{3}} \frac{\sin x - \frac{\sqrt{3}}{2}}{x - \frac{\pi}{3}}$$

$$2. \lim_{h \rightarrow 0} \frac{e^{3(x+h)} - e^{3x}}{h}$$

$$3. \lim_{h \rightarrow 0} \frac{\tan\left(\frac{\pi}{4} + h\right) - 1}{h}$$

$$4. \lim_{h \rightarrow 0} \frac{\cos(x+h) - \cos x}{h}$$

$$5. \lim_{x \rightarrow 1} \frac{3x^2 + 4x - 7}{x - 1}$$

$$6. \lim_{x \rightarrow \frac{3\pi}{4}} \frac{\cos x - \cos\left(\frac{3\pi}{4}\right)}{x - \frac{3\pi}{4}}$$

$$7. \lim_{x \rightarrow 0} \frac{e^{x^2} - 1}{x}$$

$$8. \lim_{x \rightarrow 1} \frac{\arctan x - \frac{\pi}{4}}{x - 1}$$

$$9. \lim_{h \rightarrow 0} \frac{\sec(x+h) - \sec x}{h}$$

$$10. \lim_{h \rightarrow 0} \frac{\arcsin\left(\frac{1}{2} + h\right) - \frac{\pi}{6}}{h}$$

$$11. \text{ Given } \lim_{h \rightarrow 0} \frac{f(2+h) - f(2)}{h} = 5, \text{ which of the following must be true? (not multiple choice)}$$

A) $f(x)$ is continuous at $x = 2$

B) $f'(2)$ exists

C) $f(x)$ is differentiable at $x = 2$

D) $f(2)$ exists

E) $f''(2)$ exists

Using the given u -substitution, determine a definite integral that would have the same value.

$$1. \ u = \sqrt{x}, \quad \int_4^9 \frac{\sin \sqrt{x}}{\sqrt{x}} dx$$

$$2. \ u = 2x + 3, \quad \int_1^3 \sqrt[3]{2x+3} dx$$

$$3. \ u = \ln x, \quad \int_1^e \frac{(\ln x)^5}{x} dx$$

$$4. \ u = 3x - 1, \quad \int_0^2 e^{3x-1} dx$$

$$5. \ u = \sqrt[3]{x}, \quad \int_0^8 \frac{e^{\sqrt[3]{x}}}{\sqrt[3]{x^2}} dx$$

$$6. \ u = 3x - 2, \quad \int_2^4 \cos(3x-2) dx$$

Use the given information to determine an equivalent equation involving a definite integral.

$$7. \ \int_2^4 f(2x) dx = 12$$

$$8. \ \int_1^3 f(2x-3) dx = 5$$

$$9. \ \int_3^6 f\left(\frac{x}{3}\right) dx = 6$$

$$10. \ \int_2^5 f(2-x) dx = 4$$

$$11. \ \int_4^6 f\left(\frac{x}{2} + 1\right) dx = 3$$

$$12. \ \int_0^4 f(e^{3x}) \cdot e^{3x} dx = -3$$