AP Calculus Mock Exam

AB 1

The continuous function f has domain $-2 \le x \le 9$. The graph of f, consisting of three line segments and two quarter circles, is shown in the figure.



Let g be the function defined by $g(x) = \int_0^x f(t) dt$ for $-2 \le x \le 9$.

- (a) Find the *x*-coordinate of each critical point of *g* on the interval $-2 \le x \le 9$.
- (b) Classify each critical point from part (a) as the location of a relative minimum, a relative maximum, or neither for g. Justify your answers.
- (c) For $-2 \le x \le 9$, on what open intervals is g increasing and concave down? Give a reason for your answer.
- (d) Find the value of g(-1). Show the computations that lead to your answer.
- (e) Find the value of g(2). Show the computations that lead to your answer.
- (f) Find the absolute maximum value of g over the interval $-2 \le x \le 5$.
- (g) Find the value of g''(6), or explain why it does not exist.
- (h) Must there exist a value of d, for 0 < d < 2, such that g'(d) is equal to the average rate of change of g over the interval $0 \le x \le 2$? Justify your answer.
- (i) Find $\lim_{x\to 0} \frac{3x + g(x)}{\sin x}$. Show the computations that lead to your answer.
- (j) The function h is defined by $h(x) = x \cdot g(x^2)$. Find $h'(\sqrt{2})$. Show the computations that lead to your answer.